IOPscience

Home Search Collections Journals About Contact us My IOPscience

Magnetic and electron transport properties of the rare earth cobaltates,

 $La_{0.7-x}Ln_xCa_{0.3}CoO_3$ (Ln = Pr, Nd, Gd and Dy): a case of phase separation

This article has been downloaded from IOPscience. Please scroll down to see the full text article. 2004 J. Phys.: Condens. Matter 16 7955 (http://iopscience.iop.org/0953-8984/16/45/018)

View the table of contents for this issue, or go to the journal homepage for more

Download details: IP Address: 129.252.86.83 The article was downloaded on 27/05/2010 at 19:02

Please note that terms and conditions apply.

J. Phys.: Condens. Matter 16 (2004) 7955-7966

PII: S0953-8984(04)83560-4

Magnetic and electron transport properties of the rare earth cobaltates, $La_{0.7-x}Ln_xCa_{0.3}CoO_3$ (Ln = Pr, Nd, Gd and Dy): a case of phase separation

Asish K Kundu¹, K Ramesha², Ram Seshadri² and C N R Rao^{1,3}

 ¹ Chemistry and Physics of Materials Unit, Jawaharlal Nehru Centre for Advanced Scientific Research, Jakkur PO, Bangalore-560064, India
² Materials Department, University of California, Santa Barbara, CA 93106, USA

E-mail: cnrrao@jncasr.ac.in

Received 13 July 2004, in final form 27 August 2004 Published 29 October 2004 Online at stacks.iop.org/JPhysCM/16/7955 doi:10.1088/0953-8984/16/45/018

Abstract

Magnetic and electrical properties of four series of rare earth cobaltates of the formula $La_{0.7-x}Ln_xCa_{0.3}CoO_3$ with Ln = Pr, Nd, Gd and Dy have been investigated. Compositions close to x = 0.0 contain large ferromagnetic clusters or domains, and show Brillouin-like behaviour of the field-cooled DC magnetization data with fairly high ferromagnetic T_c values, besides low electrical resistivities with near-zero temperature coefficients. When x > 0.0, the zero-field-cooled data generally show a non-monotonic behaviour with a peak at a temperature slightly lower than T_c . The compositions near x = 0.0show a prominent peak corresponding to the T_c in the AC susceptibility data. The ferromagnetic T_c varies linearly with x or the average radius of the Asite cations, $\langle r_A \rangle$. With increase in x or decrease in $\langle r_A \rangle$, the magnetization value at any given temperature decreases markedly and the AC susceptibility measurements show a prominent transition arising from small magnetic clusters with some characteristics of a spin glass. Electrical resistivity increases with increase in x, showing a significant increase around a critical value of x or $\langle r_A \rangle$, at which composition the small clusters also begin to dominate. These properties can be understood in terms of a phase separation scenario wherein large magnetic clusters give way to smaller ones with increase in x, with clusters of both types being present in certain compositions. The changes in magnetic and electrical properties occur in parallel since the large ferromagnetic clusters are hole rich and the small clusters are hole poor. Variable range hopping seems to occur at low temperatures in these cobaltates.

 3 Author to whom any correspondence should be addressed.

0953-8984/04/457955+12\$30.00 © 2004 IOP Publishing Ltd Printed in the UK

1. Introduction

Rare earth manganates of the general formula $Ln_{1-x}A_xMnO_3$ (Ln = rare earth, A = alkaline earth), possessing the perovskite structure, exhibit interesting properties such as colossal magnetoresistance, charge ordering and electronic phase separation [1-5]. These properties of the manganates are strongly influenced by the average radius of the A-site cations, $\langle r_A \rangle$. It has been found recently that manganates of the type $La_{0.7-x}Ln_xCa_{0.3}MnO_3$ (Ln = Pr, Nd, Gd, Y) undergo electronic phase separation beyond a critical composition x_c . While the $x < x_c$ compositions exhibit ferromagnetism and metallicity, materials with $x > x_c$ are nonmagnetic insulators, with the magnetic moment dropping sharply in these compositions [6-9]. Such changes in properties in a series of manganates where the carrier concentration or the Mn⁴⁺/Mn³⁺ ratio is kept constant are definitely noteworthy. Perovskite cobaltates of the type $Ln_{1-x}A_xCoO_3$ (Ln = rare earth, A = alkaline earth) are in many ways similar to the manganates [10-13]. Accordingly, many of the cobaltates show ferromagnetism and metallicity depending on the composition and the size of the A-site cations. The cobaltates also show some unusual features in their magnetic properties. Thus Itoh et al [14] find that $La_{1-x}Sr_xCoO_3$ shows spin-glass behaviour when $0.0 \le x \le 0.18$ and cluster-glass behaviour when $0.18 \le x \le 0.5$. Ganguly *et al* [15] reported long-range freezing of superparamagnetic clusters when x < 0.3. For x = 0.5, a cluster-glass magnetic behaviour has been reported by Kumar et al [16] who ascribe this property to magnetocrystalline anisotropy. Wu and Leighton [17] have recently examined the properties of $La_{1-r}Sr_rCoO_3$ and suggest that the system is best described as one dominated by glassy ferromagnetism and magnetic phase separation. We considered it important to investigate the magnetic and electron transport properties of cobaltates of the type $La_{0,7-x}Ln_xCa_{0,3}CoO_3$ (Ln = Pr, Nd, Gd or Dy), in view of the comparable natures of the cobaltates and the manganates, and also because of the likelihood that phase separation may occur in the cobaltate system as well because of the presence of strongly correlated electrons [5]. While the carrier concentration remains constant in La_{0.7-x}Ln_xCa_{0.3}CoO₃, the $\langle r_A \rangle$ and the associated factors vary. Furthermore, the Ca-substituted cobaltates were considered more likely to exhibit phase separation and related effects due to the smaller $\langle r_A \rangle$ or the eg bandwidth compared to the Sr-substituted materials.

2. Experimental procedure

Polycrystalline samples of La_{0.7-x}Ln_xCa_{0.3}CoO₃ (Ln = Pr, Nd, Gd, or Dy), were prepared by the conventional ceramic method. Stoichiometric mixtures of the respective rare earth oxides, alkaline earth carbonates and Co₃O₄ were weighed in the desired proportions and milled for a few hours with propanol. After the mixed powders were dried, they were calcined in air at 950 °C and this was followed by heating at 1000 and 1100 °C for 12 h in air. The powders thus obtained were pelletized and the pellets sintered at 1200 °C for 24 h in an oxygen atmosphere. To improve the oxygen stoichiometry, the samples were annealed in an oxygen atmosphere below 900 °C and cooled gradually. The oxygen stoichiometry was determined by iodometric titrations. The error in the determination of the oxygen content was ±0.02. The oxygen stoichiometry in the cobaltates studied by us was 2.97 ± 0.03.

The phase purity of the samples was established by recording the x-ray diffraction patterns in the 2θ range of 10° – 80° with a Seifert 3000 TT diffractometer, employing Cu K α radiation. The unit cell parameters of La_{0.7-x}Ln_xCa_{0.3}CoO₃ (Ln = Pr, Nd, Gd, Dy) are listed in table 1 along with the weighted average radii $\langle r_A \rangle$. The $\langle r_A \rangle$ values were calculated using the Shannon radii for 12-coordination in the case of rhombohedral cobaltates, and for 9-coordination in the case of the orthorhombic ones. Magnetization (*M*) measurements were made over the 5–300 K

Composition <i>x</i>	$\langle r_{\rm A} \rangle$ (Å)	Space group	Lattice parameters (Å)			V
			а	b	С	(Å ³)
0.0	1.354	RĪC	5.3906	_	_	111.6
		L	n = Pr			
0.1	1.347	RĪC	5.3869	_	_	111.2
0.2	1.340	RĪC	5.3837	_	_	111.0
0.3	1.194	Pnma	5.3836	7.5858	5.3679	219.2
0.5	1.187	Pnma	5.3723	7.5686	5.3663	218.2
0.6	1.183	Pnma	5.3652	7.5731	5.3593	217.8
0.7	1.179	Pnma	5.3577	7.5774	5.3436	216.9
		L	n = Nd			
0.1	1.345	RĪC	5.3784	_	_	110.7
0.2	1.336	$R\bar{3}C$	5.3761	_	_	110.6
0.3	1.189	Pnma	5.3795	7.5867	5.3732	219.3
0.4	1.184	Pnma	5.3700	7.5741	5.3642	218.4
0.49	1.179	Pnma	5.3667	7.5766	5.3641	218.1
0.7	1.168	Pnma	5.346	7.5638	5.3287	215.5
		L	n = Gd			
0.1	1.338	RĪC	5.3797	_	_	110.7
0.2	1.322	RĪC	5.3785	_	_	110.4
0.24	1.179	Pnma	5.3838	7.5846	5.3797	219.7
0.3	1.1725	Pnma	5.3813	7.5814	5.3624	218.8
		L	n = Dy			
0.1	1.337	RĪC	5.3759	_	_	110.1
0.195	1.179	Pnma	5.3960	7.5990	5.3729	220.3
0.3	1.165	Pnma	5.3813	7.5783	5.3583	218.5

Table 1. Crystal structure data for $La_{0.7-x}Ln_xCa_{0.3}CoO_3$ (Ln = Pr, Nd, Gd or Dy).

range with a vibrating sample magnetometer (Lakeshore 7300) and with a Quantum Design MPMS 5XL magnetometer. Electrical resistivity (ρ) measurements were carried out in the 20–300 K range by the four-probe method with silver epoxy electrodes.

3. Results and discussion

In figure 1, we show the temperature dependence of the DC magnetization for a few compositions of $La_{0.7-x}Ln_xCa_{0.3}CoO_3$ (Ln = Pr, Nd). Both the zero-field-cooled (ZFC) and field-cooled (FC) data are shown in the figure. The FC curve of the x = 0.0 composition shows a Brillouin-type temperature dependence, and a T_c value of around 170 K. With increase in x, the ZFC data show lower magnetization values and a non-monotonic behaviour. Accordingly, we see a peak in the ZFC data at a temperature T_P , the peak temperature being slightly lower than the T_c value from the FC data. The maximum value of the magnetization attained and the apparent T_c value decrease with increasing x or decreasing $\langle r_A \rangle$. At large x, we notice the appearance of a shoulder-like feature in the magnetization curve, the feature becoming clearly noticeable at $x \ge 0.6$ and $x \ge 0.4$ respectively in the Pr- and Nd-substituted series of cobaltates. This feature can be seen clearly in figure 2 where the data for $Pr_{0.7}Ca_{0.3}CoO_3$

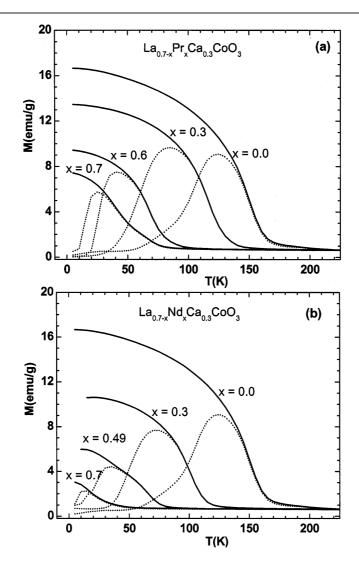


Figure 1. The temperature variation of the magnetization, M, of (a) $La_{0.7-x}Pr_xCa_{0.3}CoO_3$ and (b) $La_{0.7-x}Nd_xCa_{0.3}CoO_3$. ZFC data are shown as broken curves and FC data are shown as solid curves (at 1 kOe).

(x = 0.7) are presented. Accordingly, AC susceptibility measurements of La_{0.7}Ca_{0.3}CoO₃ (x = 0.0, $\langle r_A \rangle = 1.354$ Å) show one major frequency-independent transition around 150 K corresponding to T_c , while Pr_{0.7}Ca_{0.3}CoO₃ (x = 0.7, $\langle r_A \rangle = 1.179$ Å) shows two distinct transitions around 65 and 35 K, the latter with a greater frequency dependence, as shown in figure 3. La_{0.4}Pr_{0.3}CaO₃ ($\langle r_A \rangle = 1.194$ Å) also shows a single transition corresponding to T_c which is frequency independent just like for La_{0.7}Ca_{0.3}CoO₃. The frequency-independent high-temperature transition in Pr_{0.7}Ca_{0.3}CoO₃ is due to the large magnetic clusters (the so-called cluster glass [11, 14]) as for the x = 0.0 composition and the low-temperature transition is due to small magnetic clusters which seem to show some spin-glass characteristics. Thus, with increase in x or decrease in $\langle r_A \rangle$ in the La_{0.7-x}Ln_xCa_{0.3}CoO₃ system, the large ferromagnetic clusters seem to progressively give way to the small clusters, giving rise to

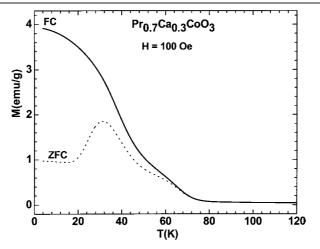
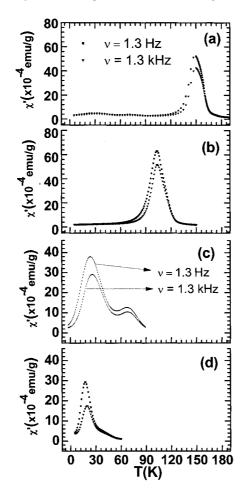


Figure 2. The temperature variation of the magnetization, M, of $Pr_{0.7}Ca_{0.3}CoO_3$ (at 100 Oe).



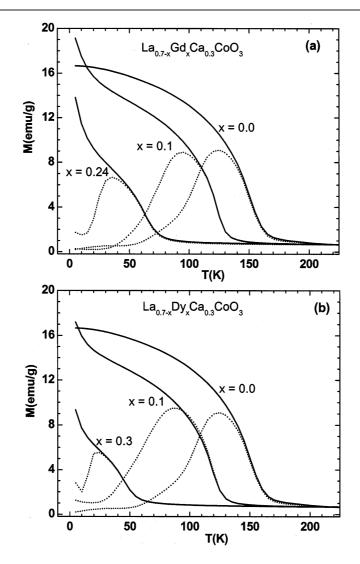


Figure 4. The temperature variation of the magnetization, M, of (a) La_{0.7-x}Gd_xCa_{0.3}CoO₃ and (b) La_{0.7-x}Dy_xCa_{0.3}CoO₃. ZFC data are shown as broken curves and FC data are shown as solid curves (1 kOe).

magnetic phase separation. The presence of very weak features at low temperatures in the AC susceptibility data for La_{0.7}Ca_{0.3}CoO₃ (figure 3(a)) indicates that the proportion of small clusters is negligible at $x \approx 0.0$. For Nd_{0.7}Ca_{0.3}CoO₃ ($\langle r_A \rangle = 1.168$ Å), on the other hand, we only see a frequency-dependent low-temperature transition around 20 K due to the small magnetic clusters (figure 3(d)).

The magnetic properties of the Gd- and Dy-substituted compositions, $La_{0.7-x}Ln_xCa_{0.3}$ CoO₃ (Ln = Gd, Dy), shown in figure 4, are similar to those of the Pr- and Nd-substituted compositions, except that at low temperatures (<30 K) an increase in magnetization is noticed. Such an increase arising from the contribution from the Gd and Dy ions has been observed earlier [18]. The T_c values obtained from FC data for the four series of cobaltates are plotted against x in figure 5. The T_c value decreases linearly with increasing x. These data can be

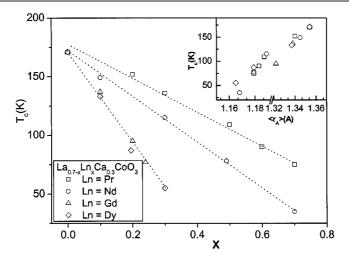


Figure 5. The variation of the ferromagnetic T_c with x in La_{0.7-x}Ln_xCa_{0.3}CoO₃. The inset shows the variation of T_c with $\langle r_A \rangle$ (Å).

rationalized in terms of the average radius of A-site cations, $\langle r_A \rangle$. Thus, a plot of T_c versus $\langle r_A \rangle$ is appreciably linear, as can be seen from the inset of figure 5.

We have recorded M-H curves of the four series of cobaltates and show typical data for two series of compounds in figure 6. The hysteresis curves do not show saturation for all the compositions. The absence of saturation is a characteristic of a glassy system. Furthermore, the remanent magnetization, M_r , decreases with increase in x or decrease in $\langle r_A \rangle$. We have plotted M_r at 50 K against $\langle r_A \rangle$ in figure 7, where we have also shown the variation of the magnetization, M, with $\langle r_A \rangle$ at this temperature. Both M and M_r increase with $\langle r_A \rangle$, but their values become rather low when $\langle r_A \rangle \lesssim 1.18$ Å.

The electrical resistivities of the cobaltates show trends which are consistent with the magnetic properties. In figure 8 we show typical resistivity data for two series of cobaltates. The temperature coefficient of resistivity changes from a near-zero value to a positive value around x_c in some of the series, but in all four series the magnitude of the resistivity shows a marked increase around a critical composition x_c or a critical radius $\langle r_A^c \rangle$ of ~1.18 Å. We observe this behaviour at x = 0.49 and 0.195 for the Nd and Dy series respectively (figure 8). In order to rationalize the resistivity data for the four series of cobaltates, we have plotted the resistivity data at 50 K against $\langle r_A \rangle$ in figure 7(c). There is a noticeable increase in the resistivity with increasing $\langle r_A \rangle$, with a change in slope around 1.18 Å. It is to be noted that below this value of the A-site cation radius, electronic phase separation and charge ordering occur in the rare earth manganates [9]. The $\langle r_A \rangle$ value of 1.18 Å in the cobaltates corresponds to $x \approx 0.6, 0.49, 0.24$ and 0.195 respectively in the Pr-, Nd-, Gd-and Dy-substituted series of cobaltates and we denote these compositions as x_c . It appears that the small magnetic cluster regime becomes prominent around x_c or $\langle r_A^c \rangle$. Even though the low-temperature peak in the AC susceptibility data is frequency dependent, the small magnetic cluster regime at small $\langle r_A \rangle$ in the $La_{0.7-x}Ln_xCa_{0.3}CoO_3$ system cannot be strictly considered to be that of a spin glass since we do not observe a logarithmic or exponential decay of the isothermal remanent magnetization. We can certainly consider the regime to be magnetically inhomogeneous. The inhomogeneous nature of the cobaltates prevails over the entire range of compositions (x = 0.0-0.7). It seems that around a composition close to x_c or $\langle r_A^c \rangle$, there is a marked change in the distribution of the magnetic species. Thus, when $x < x_c$ or $\langle r_A \rangle > \langle r_A^c \rangle$, relatively large ferromagnetic clusters

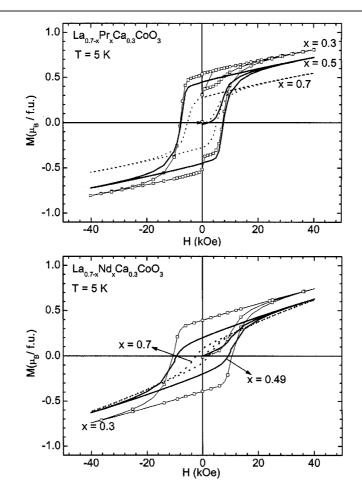


Figure 6. Typical hysteresis curves of $La_{0.7-x}Ln_xCa_{0.3}CoO_3$ at 5 K (Ln = Pr, Nd).

or domains are present in the system, resulting in large magnetization and T_c values. When $x > x_c$ or $\langle r_A \rangle < \langle r_A^c \rangle$, the magnetic clusters become small in size. The ferromagnetic clusters being hole rich, the electrical resistivity data show changes around the same compositions as the magnetization data, the compositions with $\langle r_A \rangle > \langle r_A^c \rangle$ exhibiting lower resistivities and near-zero temperature coefficients of resistivity. While one may treat the change in the nature of magnetic species around x_c or $\langle r_A^c \rangle$ as a mere change in size distribution, we consider it more appropriate to treat it as a case of phase separation since we observe more than one transition in the AC susceptibility data and the resistivity changes parallel the changes in the magnetic properties. The phase separated regime here involves the coexistence of large ferromagnetic clusters which are hole rich and small clusters which are hole poor.

It is instructive to examine the nature of the spin states of cobalt in the $La_{0.7-x}Ln_xCa_{0.3}CoO_3$ system. We can estimate the magnetic moment of the cobalt ion from the inverse magnetic susceptibility data at high temperatures (180–300 K). The susceptibility value and the slope of the inverse susceptibility–temperature plot give an average magnetic moment value of 4.5 μ_B per cobalt ion for the whole series of cobaltates. This value suggests that in the 180–300 K range, the cobalt ions are in the intermediate-spin (IS) and or high-spin (HS) states. The IS and HS states of Co³⁺ correspond to the electronic configurations

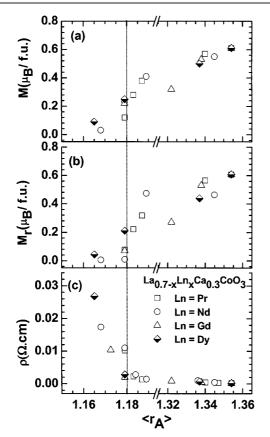


Figure 7. The variation of (a) the magnetic moment, μ_B , (b) the remanent magnetization, M_r , and (c) the electrical resistivity, ρ , in La_{0.7-x}Ln_xCa_{0.3}CoO₃ at 50 K with $\langle r_A \rangle$ (Å) (Ln = Pr, Nd, Gd and Dy).

 $t_{2g}^5 e_g^1 (S = 1)$ and $t_{2g}^4 e_g^2 (S = 2)$ respectively, and those of Co⁴⁺ to $t_{2g}^4 e_g^1 (S = 3/2)$ and $t_{2g}^3 e_g^2 (S = 5/2)$. Investigations of the spin state transitions in the cobaltates have shown that at high temperatures, the cobalt ions are mostly in the IS or the HS state [13]. At low temperatures, some of the cobalt ions may go to the low-spin (LS) state, corresponding to the $t_{2g}^6 (S = 0)$ and $t_{2g}^5 (S = 1/2)$ configurations in Co³⁺ and Co⁴⁺ ions respectively. The ferromagnetic clusters present prominently at $x < x_c$ or $\langle r_A \rangle > \langle r_A^c \rangle$ involve cobalt ions in the IS or HS states. The ferromagnetic regime will therefore be hole rich, the size of the clusters or the domains decreasing with increasing x or decreasing $\langle r_A \rangle$. We would, therefore, expect a magnetic percolation threshold as well as electrical percolation in the system. We find that a plot of log ρ versus log $|\langle r_A \rangle - \langle r_A^c \rangle|$ is linear with a negative slope of around 0.5 at 50 K.

We have explored whether the resistivity behaviour of $La_{0.7-x}Ln_xCa_{0.3}CoO_3$ conforms to activated hopping, defined by $\log \rho \propto (1/T^n)$ where n = 1, 2 or 4. Here, n = 1 corresponds to a simple Arrhenius behaviour. When n = 2, the hopping is referred to as nearest-neighbour hopping (NNH), controlled by Coulombic forces. When n = 4, there would be variable range hopping (VRH) and the hopping dynamics is controlled by the collective excitation of the charge carriers [19, 20]. The resistivity data in the 49–200 K region could be fitted to a $T^{-1/2}$ dependence with the standard deviation varying between 0.008 and 0.016. The standard

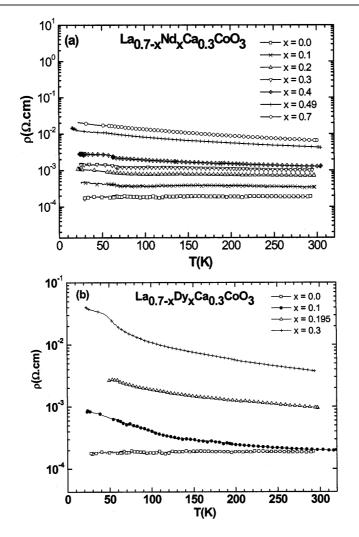


Figure 8. The temperature variation of the electrical resistivity, ρ , of La_{0.7-x}Ln_xCa_{0.3}CoO₃ (Ln = Nd and Dy).

deviation for the $T^{-1/4}$ fits is generally much smaller (0.005–0.012). In figure 9, we show typical fits to the $T^{-1/4}$ law. The occurrence of VRH in the cobaltates is consistent with the earlier studies of Rao *et al* [21, 22] on the rare earth cobaltates.

4. Conclusions

The present investigation of the magnetic and electrical properties of $La_{0.7-x}Ln_xCa_{0.3}CoO_3$ (Ln = Pr, Nd, Gd or Dy) can be understood in terms of a phase separation scenario wherein large carrier-rich ferromagnetic clusters and carrier-poor smaller clusters coexist at some compositions. Accordingly, at large x, we observe two prominent magnetic transitions, the one at low temperatures being associated with the small clusters. Since the ferromagnetic clusters prominent at small x are hole rich, we observe a change in the electrical resistivity behaviour at a critical value x_c , where the size distribution of magnetic clusters undergoes

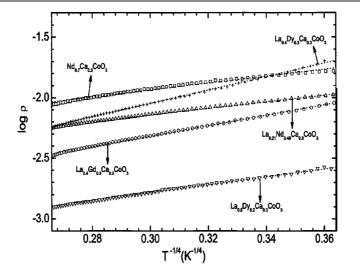


Figure 9. Fits of the resistivity data for $La_{0.7-x}Ln_xCa_{0.3}CoO_3$ for $x > x_c$ to the $T^{-1/4}$ law in the 49–200 K range. The symbols represent experimental data points and broken lines represent the linear fits.

significant changes. The critical value of x in the four series of cobaltates corresponds to the critical value of the radius, $\langle r_A^c \rangle$, of 1.18 Å, a value where rare earth manganates of the type La_{0.7-x}Ln_xCa_{0.3}MnO₃ (Ln = Nd, Gd or Y) are known to exhibit charge ordering and phase separation prominently [9]. It appears that around $\langle r_A^c \rangle$ or x_c , a significant change occurs in the eg bandwidth and the charge carriers become more localized, causing changes in the magnetic and electron transport properties. It is instructive to recall that the electrical resistivity and ferromagnetism in the cobaltates are linked to the presence of the Co³⁺–O–Co⁴⁺ species with the appropriate spin states of cobalt ions.

Acknowledgments

The authors thank BRNS (DAE), India, for support of this research. AKK wants to thank the University Grants Commission, India, for a fellowship award. The authors acknowledge the MRL facilities supported by the National Science Foundation under Award No DMROO-80034.

References

- Rao C N R and Raveau B (ed) 1998 Colossal Magnetoresistance, Charge Ordering and Related Properties of Manganese Oxides (Singapore: World Scientific)
- [2] Tokura Y (ed) 1999 Colossal Magnetoresistance Oxides (London: Gorden and Breach)
- [3] Ramirez A P 1997 J. Phys.: Condens. Matter 9 8171
- [4] Dagotto E (ed) 2003 Nanoscale Phase Separation and Colossal Magnetoresistance (Berlin: Springer)
- [5] Rao C N R and Vanitha P V 2002 Curr. Opin. Solid State Mater. Sci. 6 97
- [6] Uehara M, Mori S, Chen C H and Cheong S W 1999 *Nature* **399** 560
- [7] Lee H J, Kim K H, Kim M W, Noh T W, Kim B G, Koo T Y, Cheong S W, Wang Y J and Wei X 2002 Phys. Rev. B 65 115118
- [8] Balagurov A M, Pomjakushin Y Yu, Sheptyakov D V, Aksenov V L, Fischer P, Keller L, Gorbenko O Yu, Kaul A and Babushkina N A 2001 Phys. Rev. B 64 024420
- [9] Sudheendra L and Rao C N R 2003 J. Phys.: Condens. Matter 15 3029

- [10] Rao C N R, Parkash O, Bahadur D, Ganguly P and Nagabhushana S 1977 J. Solid State Chem. 22 353
- [11] Senaris-Rodriguez M A and Goodenough J B 1995 J. Solid State Chem. 118 323 and the references therein
- [12] Saitoh T, Mizokawa T, Fujimori A, Abbate N, Takeda Y and Takano M 1997 Phys. Rev. B 56 1290
- [13] Rao C N R, Seikh M M and Chandrabhas N 2004 Top. Curr. Chem. 234 1
- [14] Itoh M, Natori I, Kubota S and Matoya K 1994 J. Phys. Soc. Japan 63 1486
- [15] Ganguly P, Anil Kumar P S, Santosh P N and Mulla I S 1994 J. Phys.: Condens. Matter 6 533
- [16] Anil Kumar P S, Joy P A and Date S K 1998 J. Phys.: Condens. Matter 10 L487
- [17] Wu J and Leighton C 2003 Phys. Rev. B 67 174408
- [18] Tong W, Hu L, Zhu H, Tan S and Zhang Y 2004 J. Phys.: Condens. Matter 16 103
- [19] Mott N F 1990 Metal-Insulator Transitions (London: Taylor and Francis)
- [20] Shklovskii B I and Efros A L 1984 Electronic Properties of Doped Semiconductors (Berlin: Springer)
- [21] Rao C N R and Parkash O 1977 Phil. Mag. 35 1111
- [22] Rao C N R, Bhide V G and Mott N F 1975 Phil. Mag. 32 1277